

# EDEXCEL - LONDON EXAMINATIONS

Stewart House 32 Russell Square London WC1B 5DN

January 2001

Advanced Supplementary/Advanced Level

General Certificate of Education

Subject DECISION MATHEMATICS 6689

Paper No. D1



Question number	Scheme	Marks																																																								
(1) (a)	<table border="1" style="margin-left: 20px;"> <thead> <tr> <th></th> <th>1</th> <th>2</th> <th>6</th> <th>4</th> <th>5</th> <th>3</th> </tr> <tr> <th></th> <th>Office</th> <th>A</th> <th>B</th> <th>C</th> <th>D</th> <th>E</th> </tr> </thead> <tbody> <tr> <td>Office</td> <td>—</td> <td>8</td> <td>16</td> <td>12</td> <td>10</td> <td>14</td> </tr> <tr> <td>A</td> <td>8</td> <td>—</td> <td>14</td> <td>13</td> <td>11</td> <td>9</td> </tr> <tr> <td>B</td> <td>16</td> <td>14</td> <td>—</td> <td>12</td> <td>15</td> <td>11</td> </tr> <tr> <td>C</td> <td>12</td> <td>13</td> <td>12</td> <td>—</td> <td>11</td> <td>8</td> </tr> <tr> <td>D</td> <td>10</td> <td>11</td> <td>15</td> <td>11</td> <td>—</td> <td>10</td> </tr> <tr> <td>E</td> <td>14</td> <td>9</td> <td>11</td> <td>8</td> <td>10</td> <td>—</td> </tr> </tbody> </table> <p>Order of selecting edges  <i>OA, AE, EC, OD, EB</i></p> <p>Final tree</p> <p>(b) Minimum total length of cable.</p> <p><i>10 + 8 + 9 + 8 + 11 = 46</i></p>		1	2	6	4	5	3		Office	A	B	C	D	E	Office	—	8	16	12	10	14	A	8	—	14	13	11	9	B	16	14	—	12	15	11	C	12	13	12	—	11	8	D	10	11	15	11	—	10	E	14	9	11	8	10	—	<p>M I A I          O A, A E          (line order)</p> <p>M I A I          rest          (line order)</p> <p>A I</p> <p>(5)</p> <p>B I ✓ (1)</p> <p>f.c. from tree/table</p> <p style="border: 1px solid black; display: inline-block; padding: 2px;">6</p>
	1	2	6	4	5	3																																																				
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C	12	13	12	—	11	8																																																				
D	10	11	15	11	—	10																																																				
E	14	9	11	8	10	—																																																				

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(2)	<p>(a) As there are 11 names in the list the middle location is <math>[\frac{1}{2}(11+1)] = 6</math> is JONES</p> <p>Comparison 1: HUSSAIN occurs <u>before</u> JONES</p> <p>So list 2 is 1. ALLEN, 2. BALL, 3. COOPER 4. EVANS, 5 HUSSAIN.</p> <p>middle is now <math>[\frac{1}{2}(1+5)] = 3</math> is COOPER</p> <p>Comparison 2: HUSSAIN occurs <u>after</u> COOPER</p> <p>so list 3 is 4. EVANS, 5 HUSSAIN</p> <p>middle is now <math>[\frac{1}{2}(4+5)] = 5</math></p> <p>Comparison 3 HUSSAIN has been found at position 5</p> <p>(b) Maximum number of comparisons with a list of 11 names is 4</p>	<p>M I A I</p> <p>A I</p> <p>M I A I</p> <p>A I (6)</p> <p>B I C A C (1)</p> <p style="text-align: right;"><b>7</b></p>

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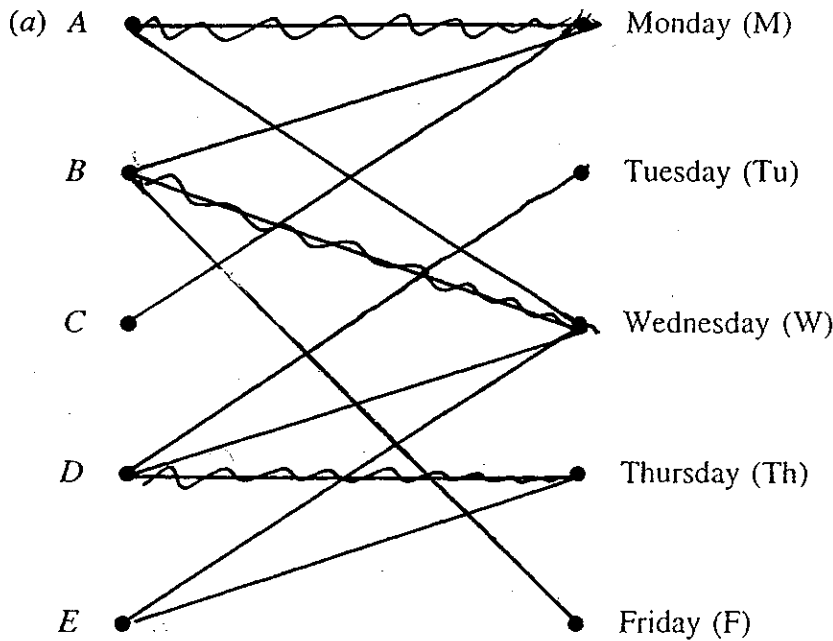
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(3)	<p>(a)</p> <table border="1" data-bbox="279 566 1066 694"> <tr> <td>vertices</td> <td>A</td> <td>B</td> <td>C</td> <td>D</td> <td>E</td> <td>F</td> </tr> <tr> <td>valency</td> <td>3</td> <td>2</td> <td>4</td> <td>3</td> <td>3</td> <td>3</td> </tr> </table> <p>Odd vertices are A, D, E and F.</p> <table border="0" data-bbox="231 750 1225 1131"> <tr> <td>Possible pairings</td> <td>Shortest routes</td> <td>Total</td> <td></td> </tr> <tr> <td>(A, F) and (D, E)</td> <td>AF + DE (60) + (90)</td> <td>150*</td> <td></td> </tr> <tr> <td>(A, E) and (D, F)</td> <td>AFGE + DGF (170) + (70)</td> <td>240</td> <td></td> </tr> <tr> <td>(A, D) and (E, F)</td> <td>ACD + EGF (120) + (110)</td> <td>230</td> <td></td> </tr> </table> <p>So repeat AF and DE</p> <p>Possible route <math>\overset{\curvearrowright}{A} \overset{\curvearrowright}{F} \overset{\curvearrowright}{E} \overset{\curvearrowright}{D} \overset{\curvearrowright}{E} \overset{\curvearrowright}{G} \overset{\curvearrowright}{D} \overset{\curvearrowright}{C} \overset{\curvearrowright}{B} \overset{\curvearrowright}{A} \overset{\curvearrowright}{C} \overset{\curvearrowright}{G} \overset{\curvearrowright}{F} \overset{\curvearrowright}{A}</math></p> <p>(b) Total length of this route                      = Total weight of edges + 150                      = 690 + 150 = 840 m</p>	vertices	A	B	C	D	E	F	valency	3	2	4	3	3	3	Possible pairings	Shortest routes	Total		(A, F) and (D, E)	AF + DE (60) + (90)	150*		(A, E) and (D, F)	AFGE + DGF (170) + (70)	240		(A, D) and (E, F)	ACD + EGF (120) + (110)	230		<p>B   cao</p> <p>M   A  </p> <p>A   ✓</p> <p>A   ✓ (5)</p> <p>M  </p> <p>A   ✓ (2)</p> <p style="text-align: right;"><b>7</b></p>
vertices	A	B	C	D	E	F																										
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Possible pairings	Shortest routes	Total																														
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(A, D) and (E, F)	ACD + EGF (120) + (110)	230																														



(4)



MARKS.

B 1  
B 1 (2)

(b)  $C - M = A - W = B - F$  (break through)  
 Changing status  
 $C = M - A = W - B - F$   
 Matching now  $D = Th, C = M, A = W, B = F$

M 1 A 1  
A 1 (3)

(c)  $E - Th = D - Tu$   
 Changing status  
 $E = Th - D = Tu$   
 So complete matching is  
 $A = W, B = F, C = M, D = Tu, E = Th$

M 1 A 1  
A 1 (3)

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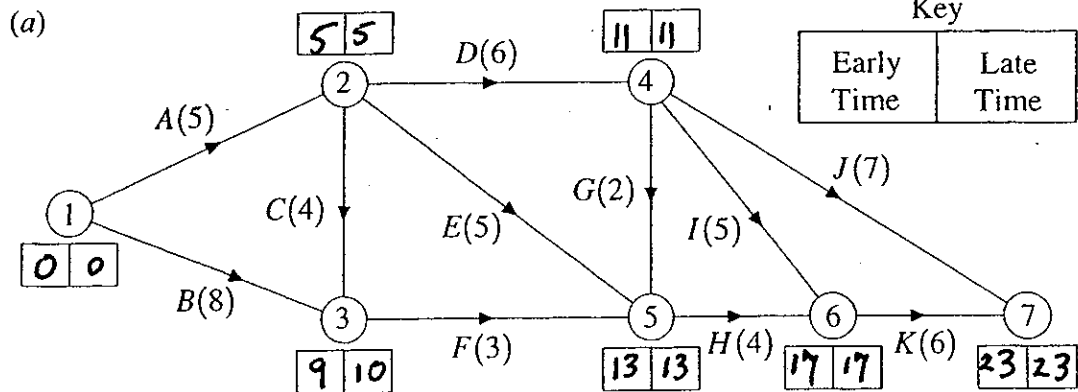
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(5)



$$e_1 = 0, \quad e_2 = 5, \quad e_3 = 9$$

$$e_4 = 11, \quad e_5 = \max(10, 12, 13) = 13$$

$$e_6 = \max(16, 17) = 17, \quad e_7 = \max(18, 23) = 23$$

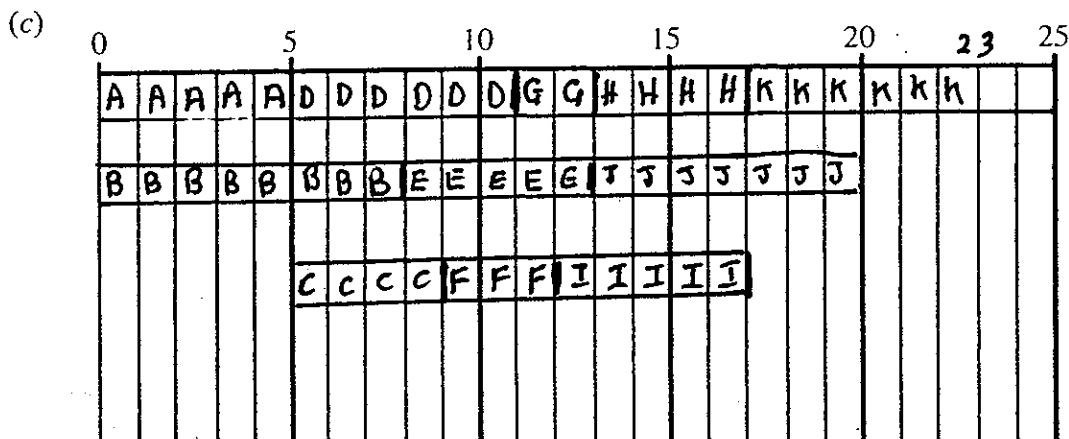
$$l_7 = 23, \quad l_6 = 17, \quad l_5 = 13$$

$$l_4 = \min(16, 12, 11) = 11, \quad l_3 = 10$$

$$l_2 = \min(6, 8, 5) = 5, \quad l_1 = \min(2, 0) = 0$$

(b) Critical activities A, D, G, H, K

Length of critical path 5 + 6 + 2 + 4 + 6 = 23



MARKS

B 1

M 1 A 1

B 1

M 1 A 1 (6)

A 1 ✓

A 1 ✓

(2)

M 1 A 1

M 1 A 2

-100

(5)

13

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- (6) (a) (i) SAET ..... 5  
 (ii) SBDT ..... 4  
 (iii) SCFT ..... 3

B 1 cas  
 B 1 cas  
 B 1 cas (3)

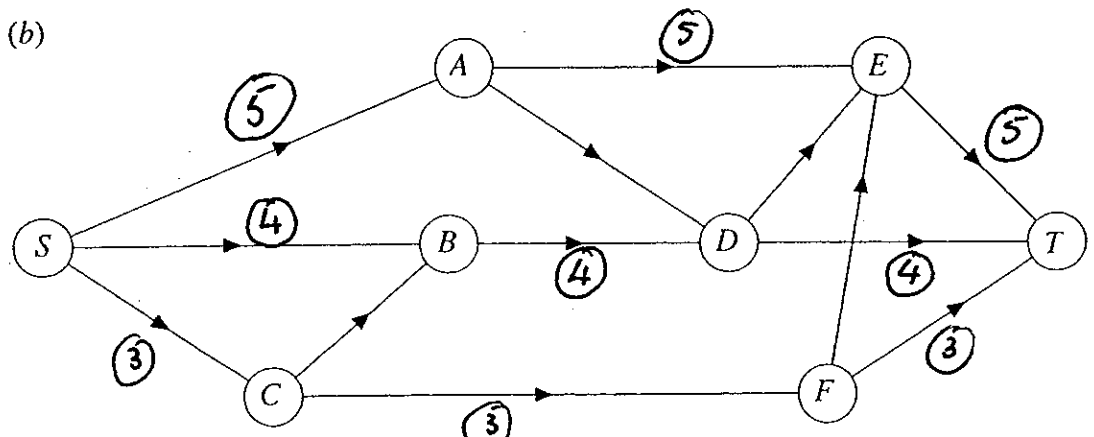


Diagram 1

B 1  
 (1)

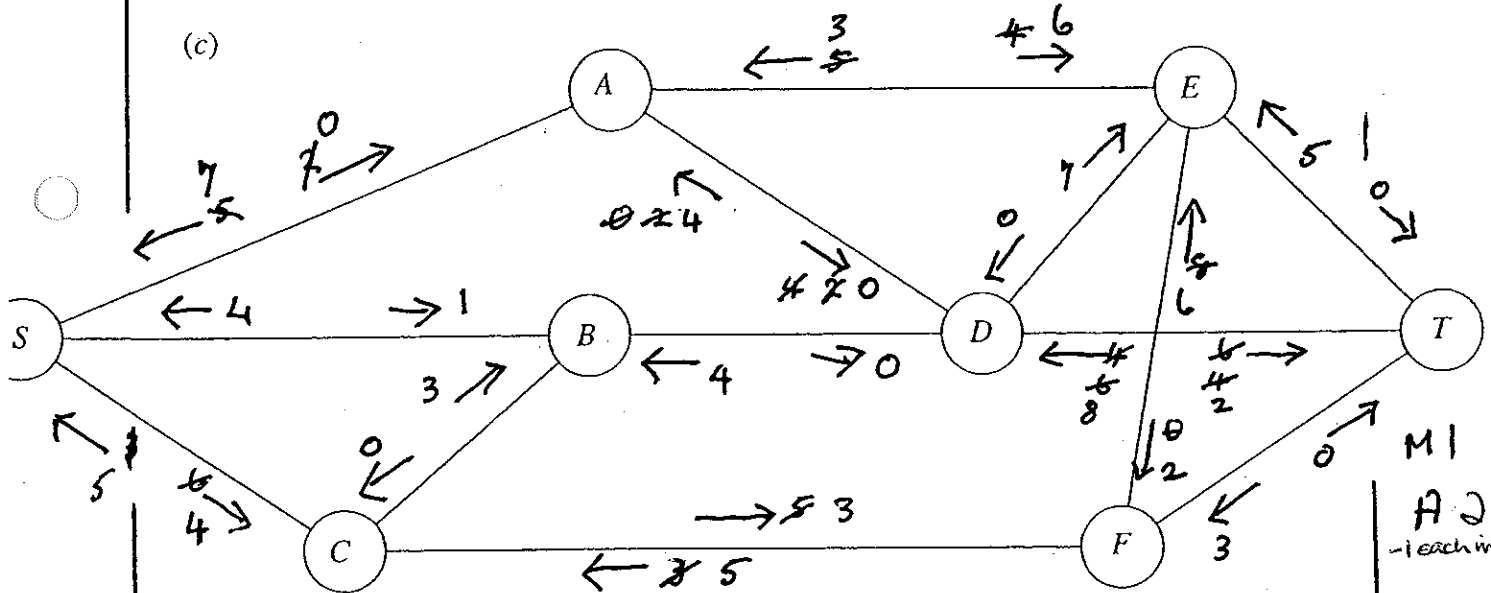


Diagram 2

M 1  
 A 2  
 -1 each incorr arc

Flow augmenting routes

- ... S A D T ... flow 2  
 ... S C F E A D T ... flow 2  
 Total flow 12 + 2 + 2 = 16

B 1  
 B 1  
 A 1 (6)

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6 cont'd  
(d)

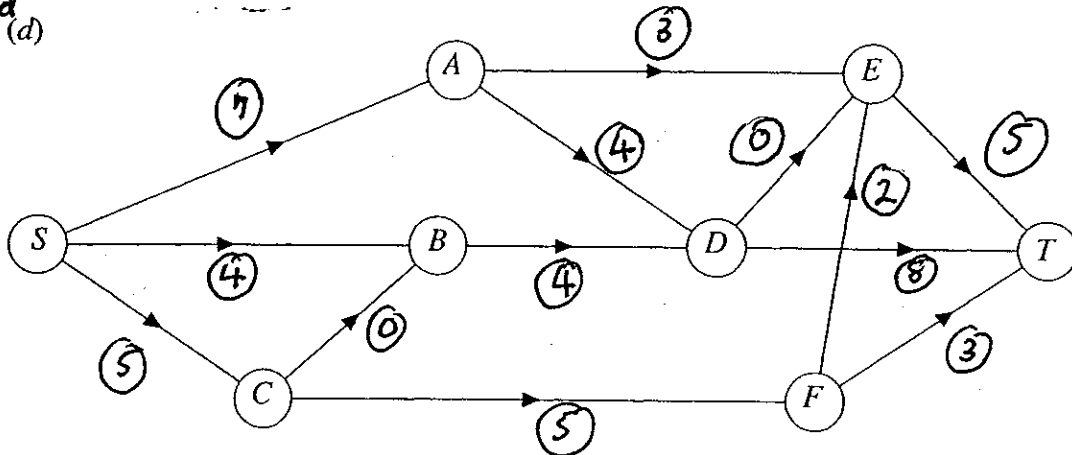


Diagram 3

- (e) There is a cut of capacity 16 consisting of  $ET$ ,  $FT$ ,  $AD$  and  $BD$ .  
 [Alt:  $ET$  is saturated and  $FT$  is saturated. Only possible route to  $T$  is then  $DT$ . But as  $AD$  and  $BD$  are saturated no flow into  $D$  is possible.]

MIAI  
(2)

MIAI  
(2)

14

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(7) (a)	<p>Cotton <math>1.x + 2y \leq 70</math> (available)</p> <p>Wool <math>3.x + 2y \leq 90</math> (available)</p> <p>Non negativity <math>x \geq 0, y \geq 0</math>.</p>	<p>31</p> <p>31 (2)</p>																								
(b)	<p>Income <math>\frac{1}{2}P</math> where <math>P = 30x + 40y</math></p> <p>Objective to maximize P</p> <p>Adding slack variables r and s</p> $x + 2y + r = 70$ $3x + 2y + s = 90$ <p>So initial tableau is</p> <table border="1" data-bbox="268 1151 1241 1422"> <thead> <tr> <th>Basic Var</th> <th>x</th> <th>y</th> <th>r</th> <th>s</th> <th>Value</th> </tr> </thead> <tbody> <tr> <td>r</td> <td>1</td> <td>②</td> <td>1</td> <td>0</td> <td>70</td> </tr> <tr> <td>s</td> <td>3</td> <td>2</td> <td>0</td> <td>1</td> <td>90</td> </tr> <tr> <td>P</td> <td>-30</td> <td>-40</td> <td>0</td> <td>0</td> <td>0</td> </tr> </tbody> </table>	Basic Var	x	y	r	s	Value	r	1	②	1	0	70	s	3	2	0	1	90	P	-30	-40	0	0	0	<p>M1</p> <p>A1</p> <p>A1 (3)</p>
Basic Var	x	y	r	s	Value																					
r	1	②	1	0	70																					
s	3	2	0	1	90																					
P	-30	-40	0	0	0																					
(c)	<p>① values row 1: <math>70/2 = 35</math> *</p> <p>row 2: <math>90/2 = 45</math></p> <p>So mixed ② is pivot</p> <p>Second tableau is then</p> <table border="1" data-bbox="300 1715 1283 2007"> <thead> <tr> <th>Basic Var</th> <th>x</th> <th>y</th> <th>r</th> <th>s</th> <th>Value</th> </tr> </thead> <tbody> <tr> <td>y</td> <td><math>\frac{1}{2}</math></td> <td>1</td> <td><math>\frac{1}{2}</math></td> <td>0</td> <td>35</td> </tr> <tr> <td>s</td> <td>②</td> <td>0</td> <td>-1</td> <td>1</td> <td>20</td> </tr> <tr> <td>P</td> <td>-10</td> <td>0</td> <td>20</td> <td>0</td> <td>1400</td> </tr> </tbody> </table>	Basic Var	x	y	r	s	Value	y	$\frac{1}{2}$	1	$\frac{1}{2}$	0	35	s	②	0	-1	1	20	P	-10	0	20	0	1400	<p>M1 A1</p> <p>M1 A1</p>
Basic Var	x	y	r	s	Value																					
y	$\frac{1}{2}$	1	$\frac{1}{2}$	0	35																					
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P	-10	0	20	0	1400																					



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4 (cont'd)	<p> <math>\ominus</math> values row 1: <math>35/\frac{1}{2} = 70</math>                      row 2: <math>20/2 = 10</math> *                      so mixed ② is pivot                      Third tableau is                 </p> <table border="1" data-bbox="252 817 1257 1108"> <thead> <tr> <th>Basic Var</th> <th>x</th> <th>y</th> <th>r</th> <th>s</th> <th>Value</th> </tr> </thead> <tbody> <tr> <td>y</td> <td>0</td> <td>1</td> <td><math>\frac{3}{4}</math></td> <td><math>-\frac{1}{4}</math></td> <td>30</td> </tr> <tr> <td>x</td> <td>1</td> <td>0</td> <td><math>-\frac{1}{2}</math></td> <td><math>\frac{1}{2}</math></td> <td>10</td> </tr> <tr> <td>P</td> <td>0</td> <td>0</td> <td>15</td> <td>5</td> <td>1500</td> </tr> </tbody> </table> <p>                     So <math>x = 10</math>, <math>y = 30</math>, <math>P = 1500</math>                      (d) <math>x + 2y = 70</math> goes through <math>(0, 35)</math> <math>(70, 0)</math>  <math>3x + 2y = 90</math> goes through <math>(0, 45)</math> <math>(30, 0)</math>                      So A is <math>(0, 35)</math> D is <math>(30, 0)</math>                      C is given by <math>x + 2y = 70</math>                      and <math>3x + 2y = 90</math>                      so <math>x = 10</math> and <math>y = 30</math> </p> <p>                     (e) Initial tableau relates to O (<math>x=0, y=0, P=0</math>)                      Second tableau relates to A (<math>x=0, y=35, P=1400</math>)                      Third tableau relates to C (<math>x=10, y=30, P=1500</math>)                 </p>	Basic Var	x	y	r	s	Value	y	0	1	$\frac{3}{4}$	$-\frac{1}{4}$	30	x	1	0	$-\frac{1}{2}$	$\frac{1}{2}$	10	P	0	0	15	5	1500	<p>MIAI</p> <p>A1</p> <p>A1(8)</p> <p>MIAI</p> <p>MIAI (4)</p> <p>B1</p> <p>B1</p> <p>B1 (3)</p>
Basic Var	x	y	r	s	Value																					
y	0	1	$\frac{3}{4}$	$-\frac{1}{4}$	30																					
x	1	0	$-\frac{1}{2}$	$\frac{1}{2}$	10																					
P	0	0	15	5	1500																					
		<p style="text-align: right;">20</p>																								